

CG – T2

Introduction to CG

L:CC, MI:ERSI

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(course and slides designed by
Verónica Costa Orvalho)

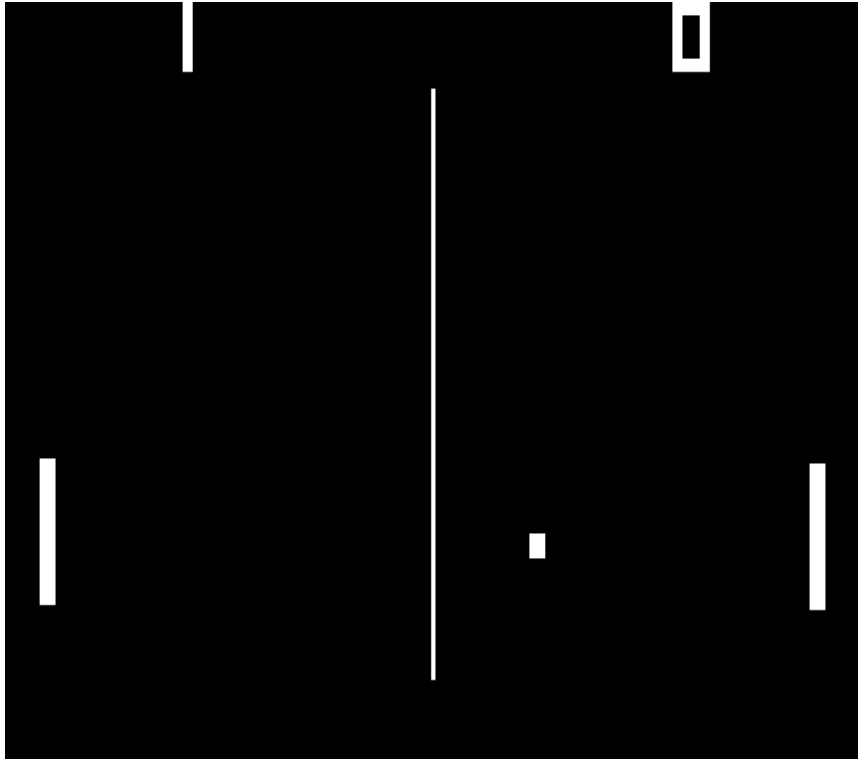
the beginning: 2D

1st CG displayed 2D graphics
(flat lines, circles, polygons)

Simple arcade games: Pong

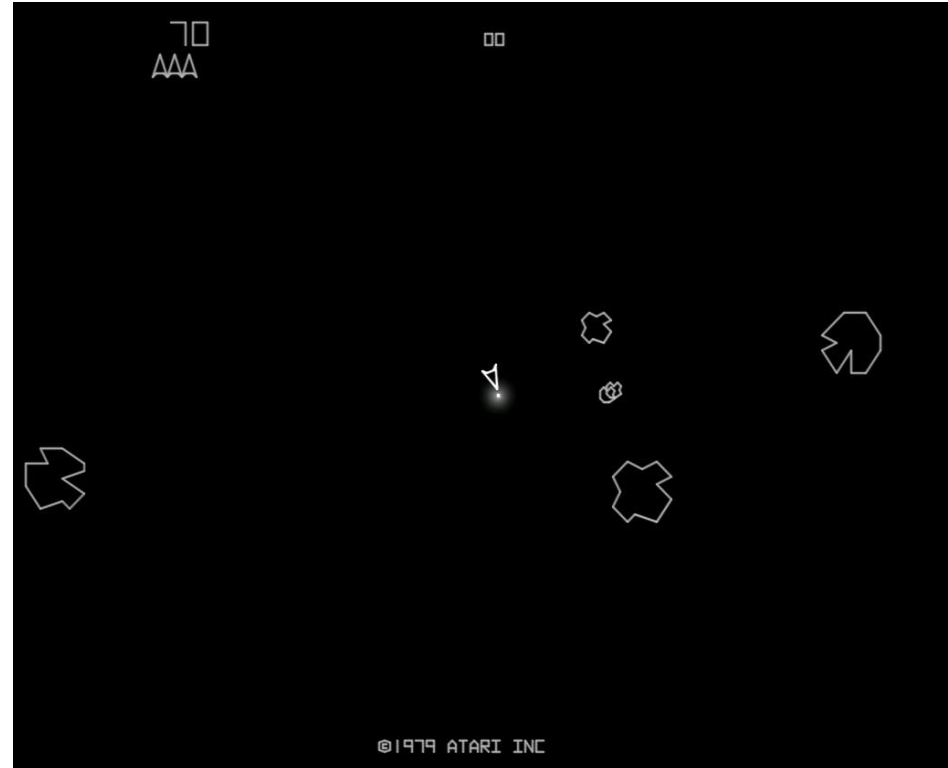
**Real-time: CG that were
animated**

pong



1972

lunar lander

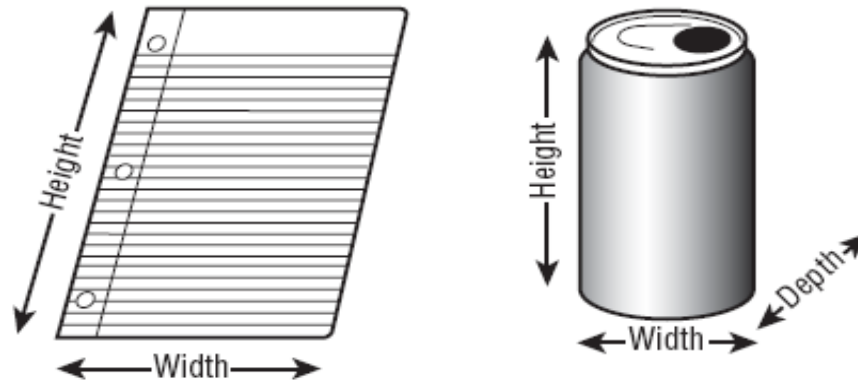


1979

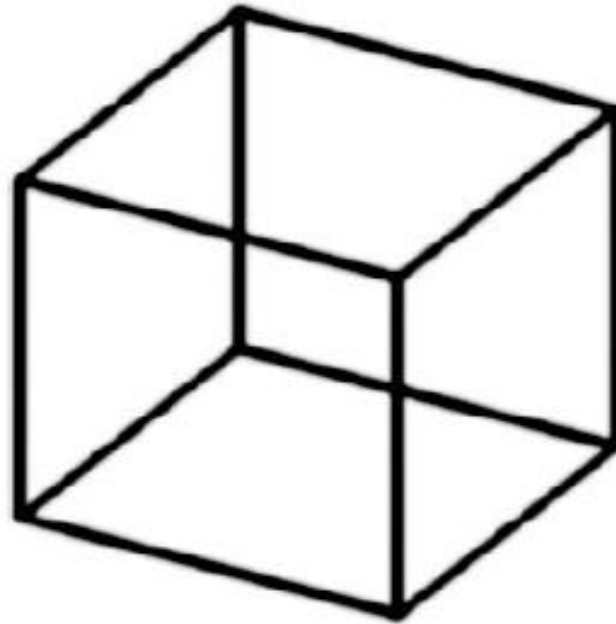
why and how 3D?

3D has 3 dimensions of measurement

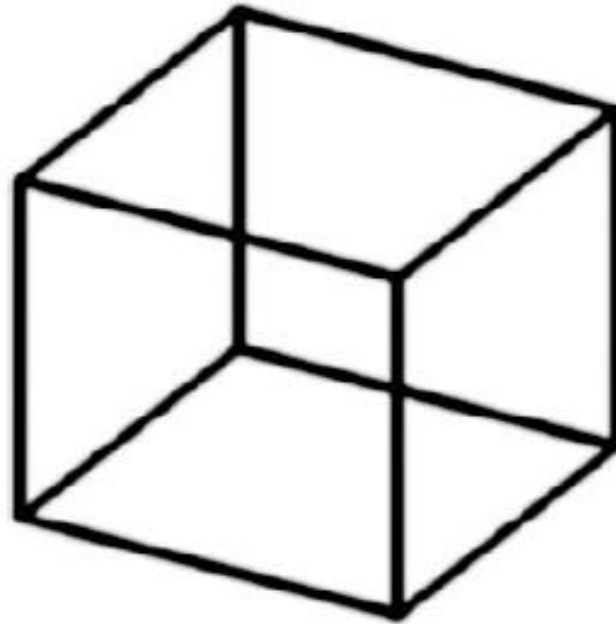
width, height and depth



what is this?



what is this?



This is a 2D image of a
drawing of a cube

3D illusion

3D computer graphics are actually 2D images on a flat screen

what makes the cube look 3D ?

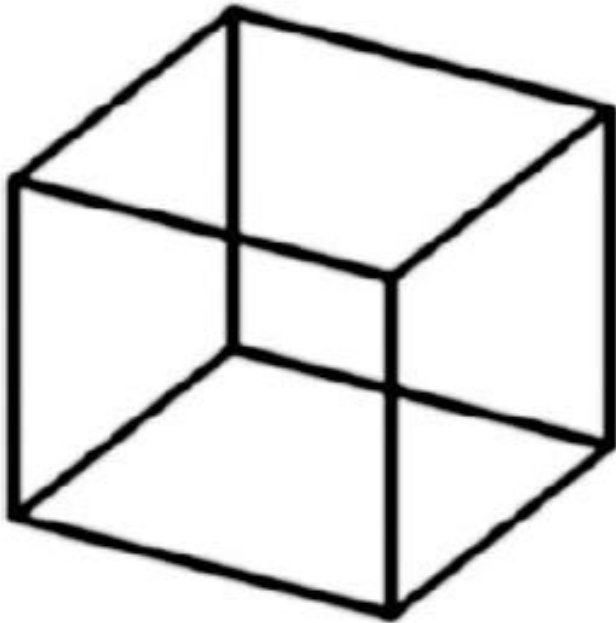
3D illusion

3D computer graphics are actually 2D images on a flat screen

what makes the cube look 3D ?
is **perspective** or the angle
between the lines (illusion)

3D illusion

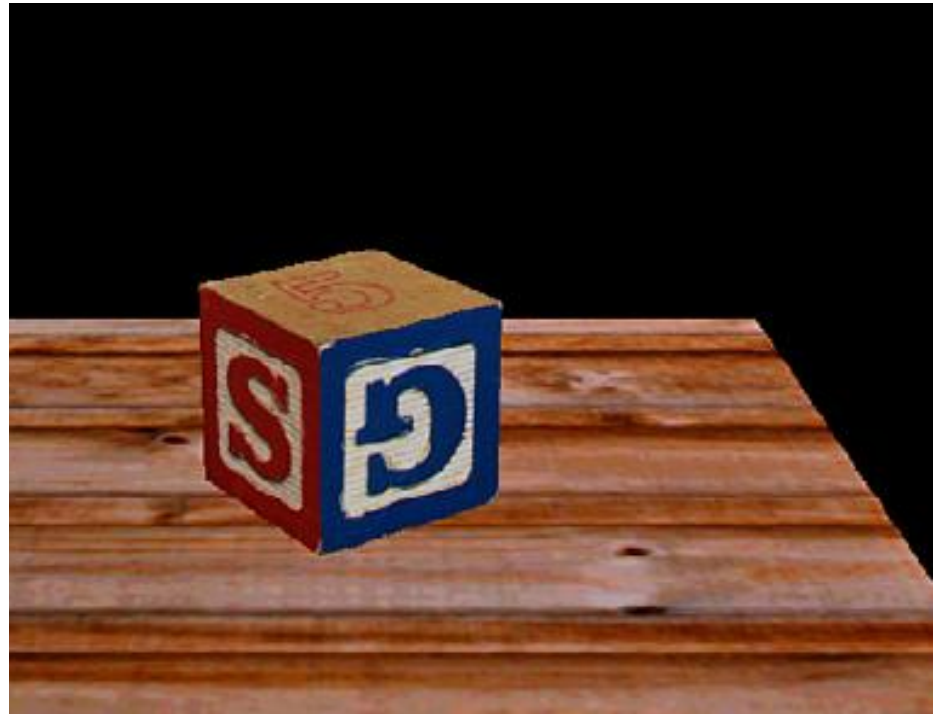
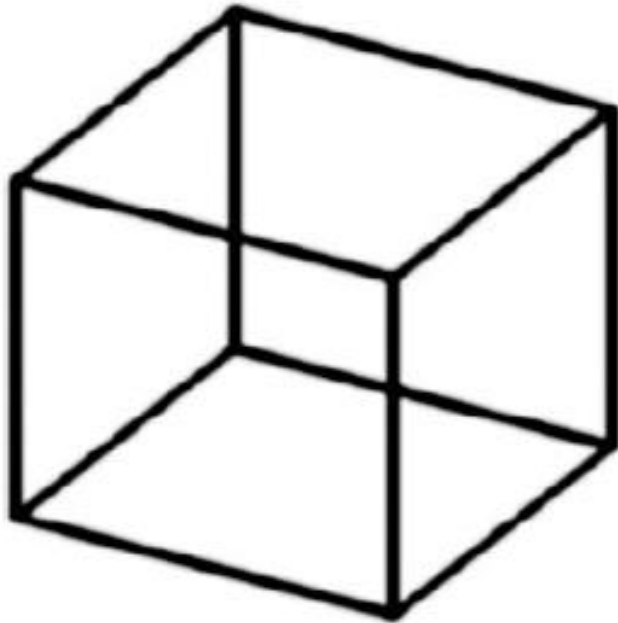
perspective is not enough



**what
else?**

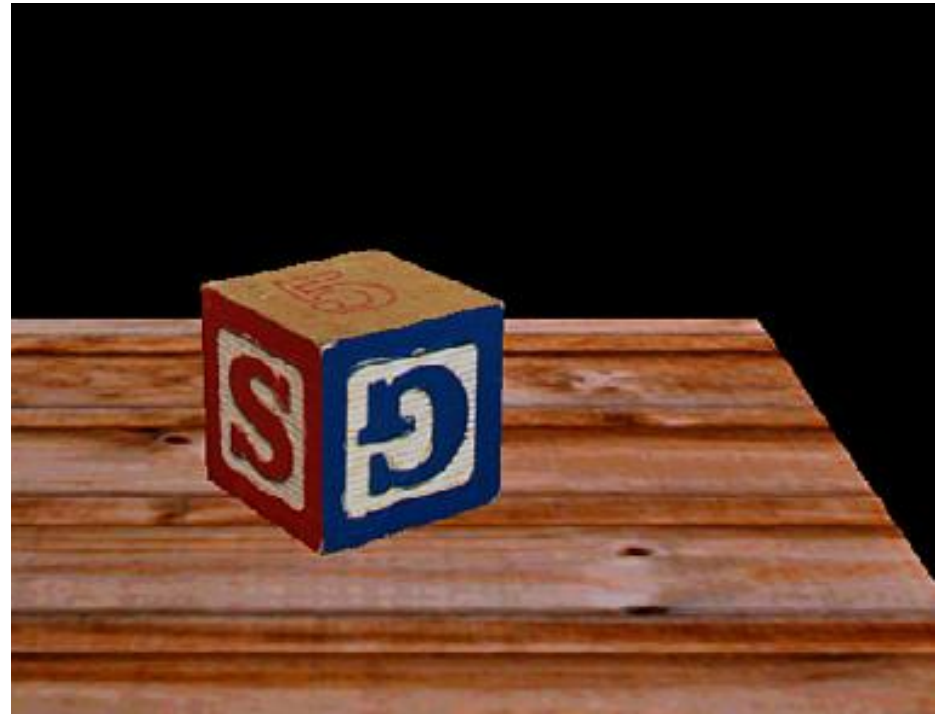
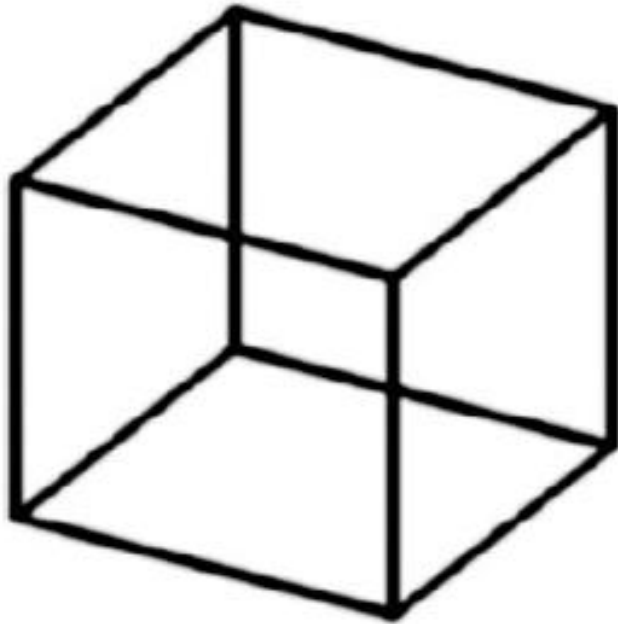
3D illusion

perspective is not enough



3D illusion

perspective is not enough

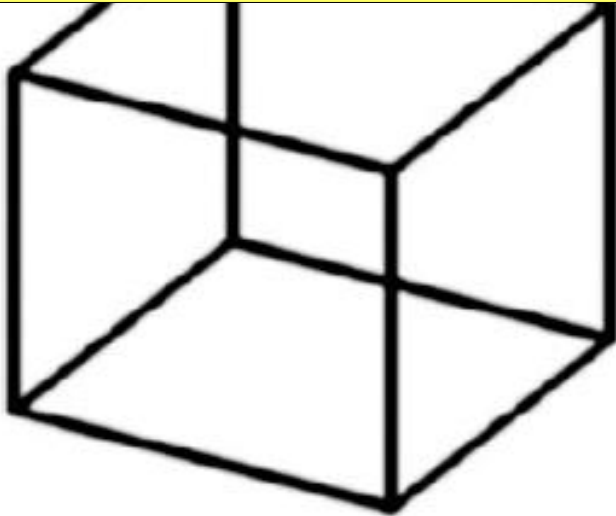


**color changes, textures,
shading, color intensity....**

3D illusion

perspective is not enough

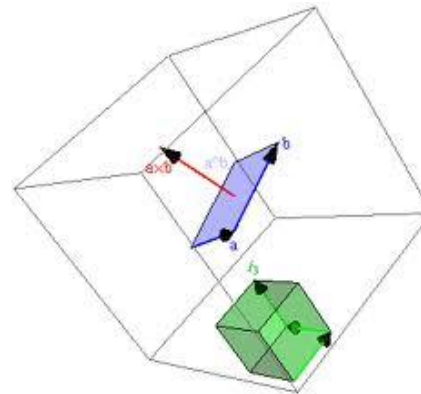
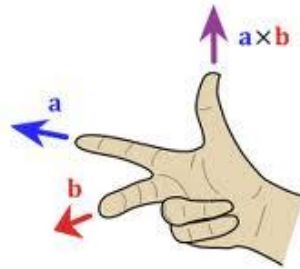
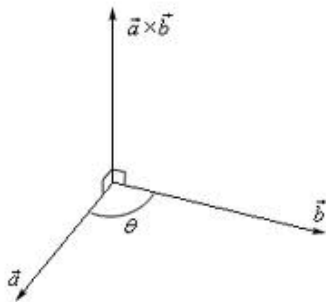
perception of a 3D image



**color changes, textures,
shading, color intensity....**

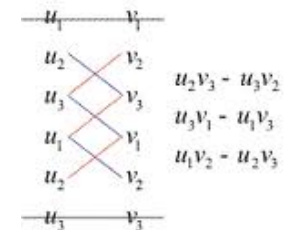
math you might need today

cross product



not commutative,
order is important

$$\begin{pmatrix} a_x \\ a_y \\ a_z \end{pmatrix} \times \begin{pmatrix} b_x \\ b_y \\ b_z \end{pmatrix} = \begin{pmatrix} a_y b_z - b_y a_z \\ a_z b_x - b_z a_x \\ a_x b_y - b_x a_y \end{pmatrix}$$



math you might need today

cross product

Vector crossproduct(Vector &v)

{

Vector vector;

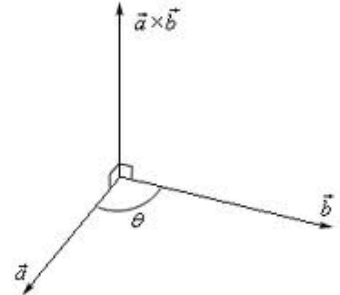
$$\text{vector.x} = (y * v.z) - (z * v.y);$$

$$\text{vector.y} = (z * v.x) - (x * v.z);$$

$$\text{vector.z} = (x * v.y) - (y * v.x);$$

return vector;

}



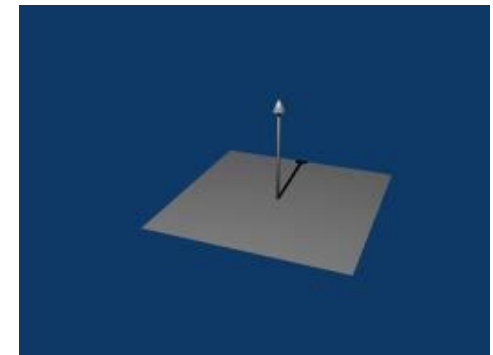
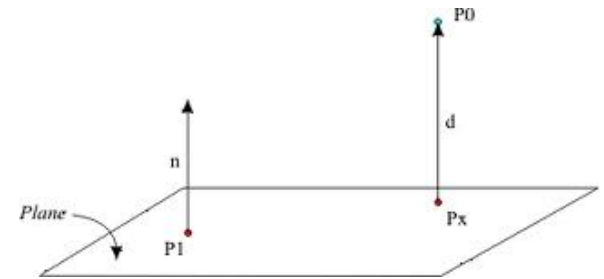
$$\begin{pmatrix} a_x \\ a_y \\ a_z \end{pmatrix} \times \begin{pmatrix} b_x \\ b_y \\ b_z \end{pmatrix} = \begin{pmatrix} a_y b_z - b_y a_z \\ a_z b_x - b_z a_x \\ a_x b_y - b_x a_y \end{pmatrix}$$

math you might need today

the plane equation

A plane is defined as:

- > a set of points perpendicular to a normal vector $\mathbf{n} = (a, b, c)$
- > that also contains the point $\mathbf{P0} = (x_0, y_0, z_0)$
- > if a point \mathbf{P} lies on the plane, then vector $\mathbf{v} = \mathbf{P} - \mathbf{P0}$ also lies on the plane
- > then $\mathbf{n} \cdot \mathbf{v} = 0$ (dot product)
 $\mathbf{n} \cdot \mathbf{v} \Rightarrow (x * v.x) + (y * v.y) + (z * v.z);$



$$A \cdot B = \|A\| \|B\| \cos \theta$$

$$a(x-x_0) + b(y-y_0) + c(z-z_0) = 0$$

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math you might need today

more about vectors

magnitude (length):

$$|a| = \text{sqrt}((ax * ax) + (ay * ay) + (az * az))$$

unit Vector – normalization

- 1 calculate its length, then,
- 2 divide each of its (xyz) components by its length.

$$x = ax/|a|$$

$$y = ay/|a|$$

$$z = az/|a|$$

$$\text{magnitued} = \text{sqrt}(9 + 1 + 4) = 3.742$$

$$x = 3.0 / 3.742 = \mathbf{0.802}$$

$$y = 1.0 / 3.742 = \mathbf{0.267}$$

$$z = 2.0 / 3.742 = \mathbf{0.534}$$

Values between [0,1]

terms you must know: the beginning

vertex: 3D point in space

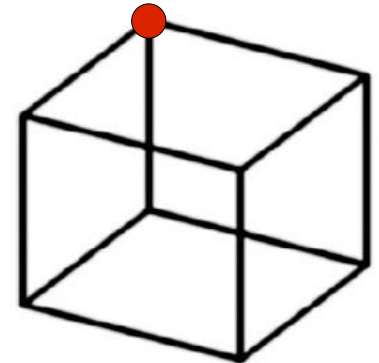
transformation matrix: move vertex around in space

projection matrix: turn 3D coordinates into 2D screen coordinates

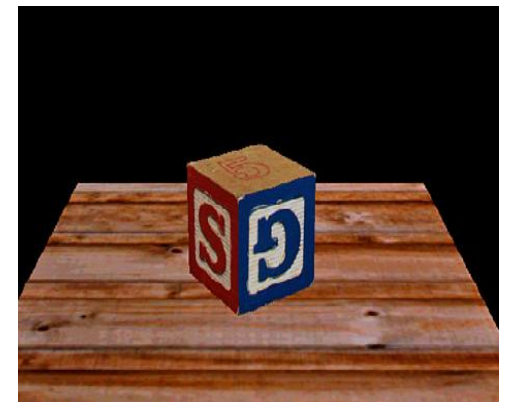
transforming points around and creating lines between them we create the 3D illusion

rasterization: drawing or filling the pixels between each vertex

vertex

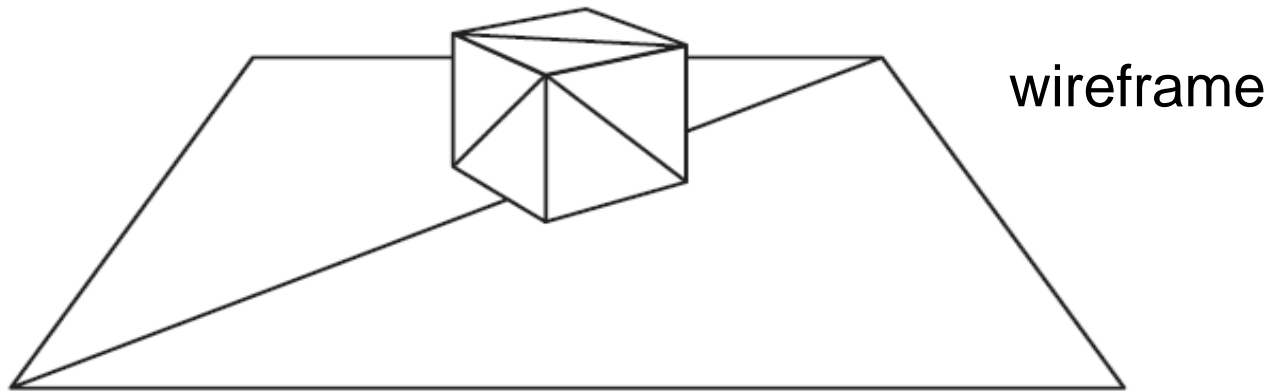


wireframe

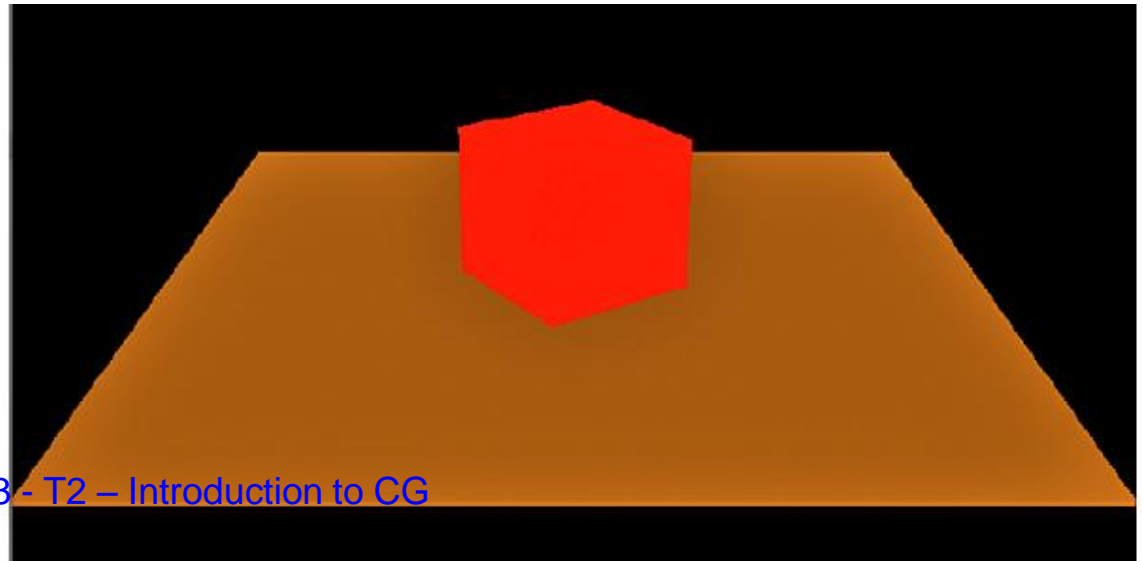


terms you must know: the beginning

rasterization:

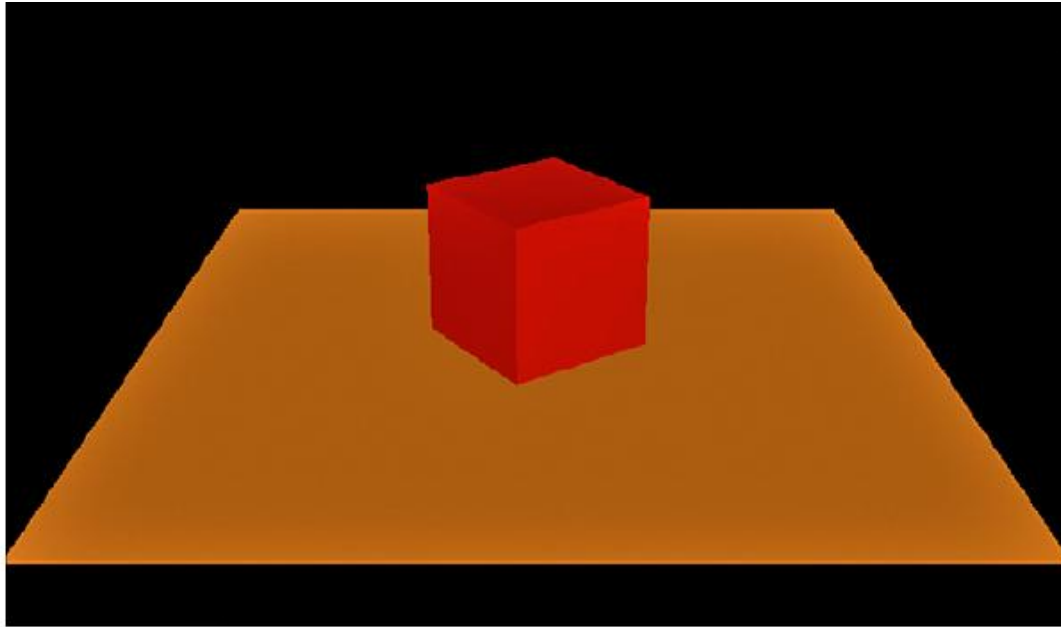


filling with
colors



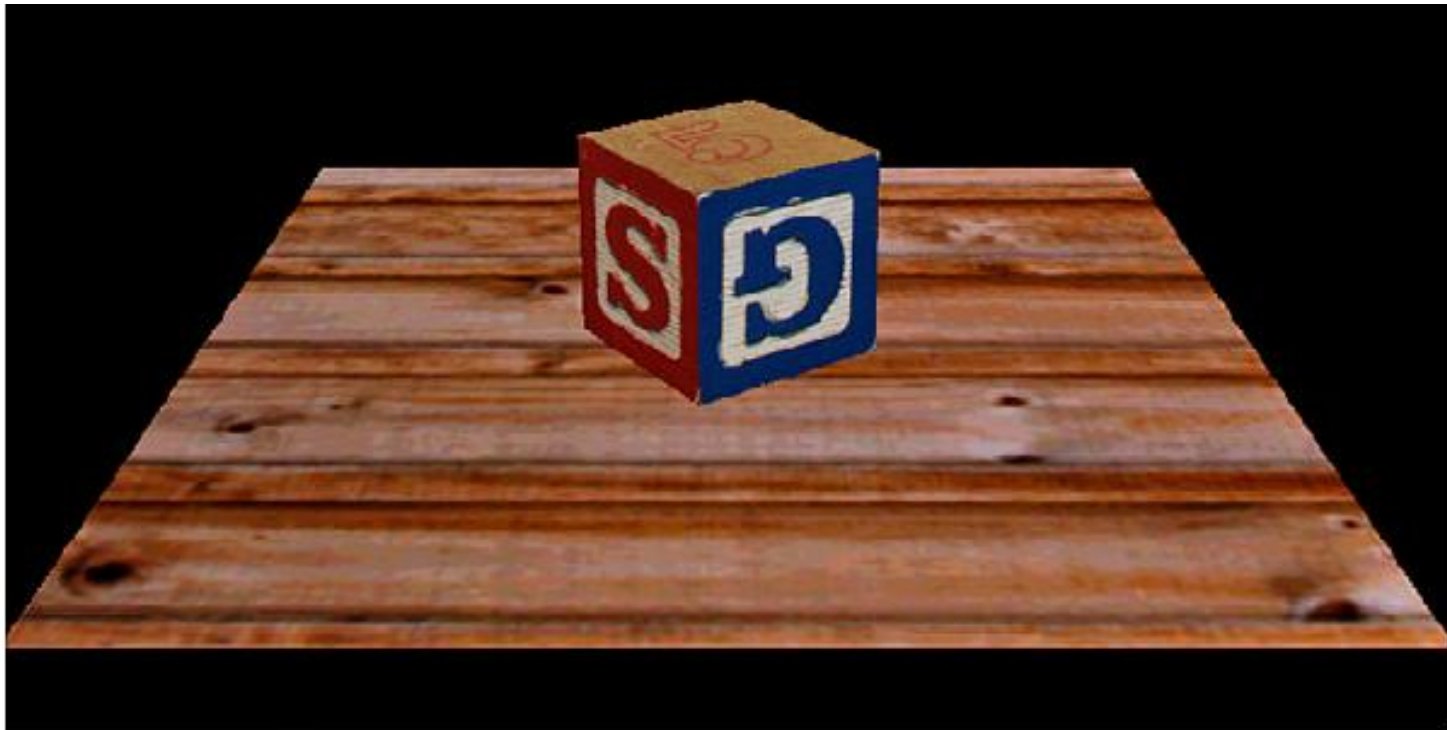
terms you must know: the beginning

Shading: varying the color values across the surface (between vertices). Create the effect of light shining on a red cube



terms you must know: the beginning

texture mapping: a picture that we map to the surface of a triangle or polygon. A texture can simulate an effect that could take thousands of triangles.



terms you must know: the beginning

blending: allows mixing different colors together. e.g. create reflections.



everything comes together

transformation + shading + texture + blending



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Summary

- We will try create the illusion of a 3D world using a 2D screen
- Humans mentally build their 3D illusion based on two 2D images (but now we only have one...)
- We need maths
- We need structure: transformation, shading, texture, blending